

# Bounding Higgs Width Through Interferometry

*work with:*

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# Outline

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- *Interference in  $gg \rightarrow H \rightarrow \gamma\gamma$*
- *Real part interference: mass shift*
- *NLO corrections to interference*
- *Bounding  $\Gamma_H$  using mass shift*
- *Conclusion*

# Higgs Production

- Dominated by gluon fusion through a top quark loop



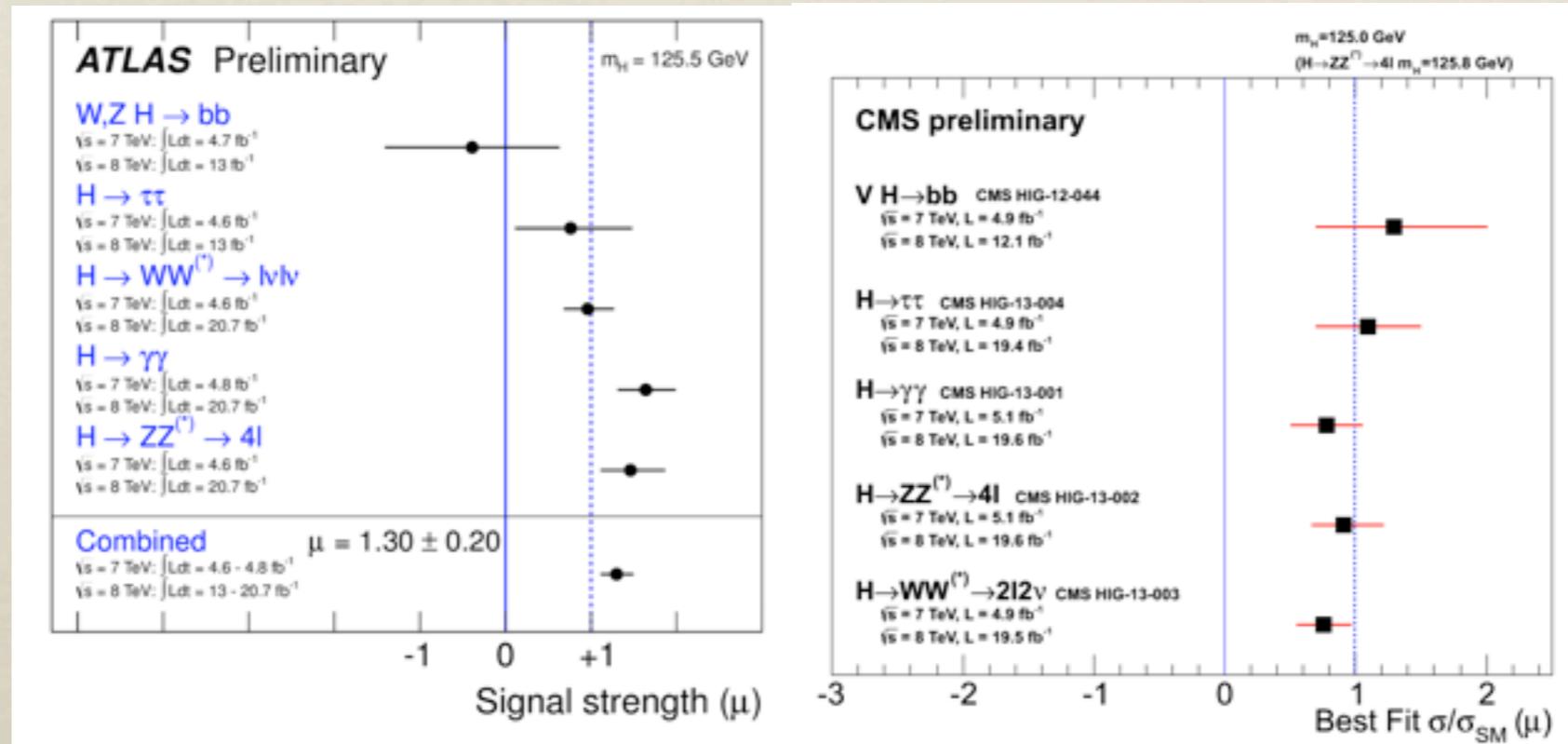
- To make higher order correction feasible, approximate top quark loop by effective  $ggH$  vertex
- Similarly, photon couples to Higgs through top quark and  $W$  boson loop, can also be approximated by effective  $\gamma\gamma H$  vertex

SM :  $b_{g,\gamma} = \frac{2}{3}, \frac{47}{9}$  at LO in heavy top/W limit

$$\mathcal{L} = - \left[ \frac{\alpha_s}{8\pi} c_g b_g G_{a,\mu\nu} G_a^{\mu\nu} + \frac{\alpha}{8\pi} c_\gamma b_\gamma F_{\mu\nu} F^{\mu\nu} \right] \frac{h}{v}$$

new physics correction

# Higgs Decay



- For  $m_H \sim 125 \text{ GeV}$ , Higgs resonance is weak
- Diphoton decay
  - excellent experimental photon energy resolution  $\Rightarrow \gamma\gamma$  signal visible even though  $\text{Br}(H \rightarrow \gamma\gamma) \sim 0.0023$
  - fully reconstructed invariant mass
- large SM background
- data in reasonable agreement with SM prediction
- Additional invisible/ undetectable decay channels could increase Higgs total width and reduce  $\gamma\gamma$  BR

# Full Diphoton Amplitude

- *Gluon pair to diphoton full amplitude*

$$\mathcal{A}_{gg \rightarrow \gamma\gamma} = -\frac{\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H}}{M_{\gamma\gamma}^2 - m_H^2 + im_H \Gamma_H} + \mathcal{A}_{\text{cont}}$$

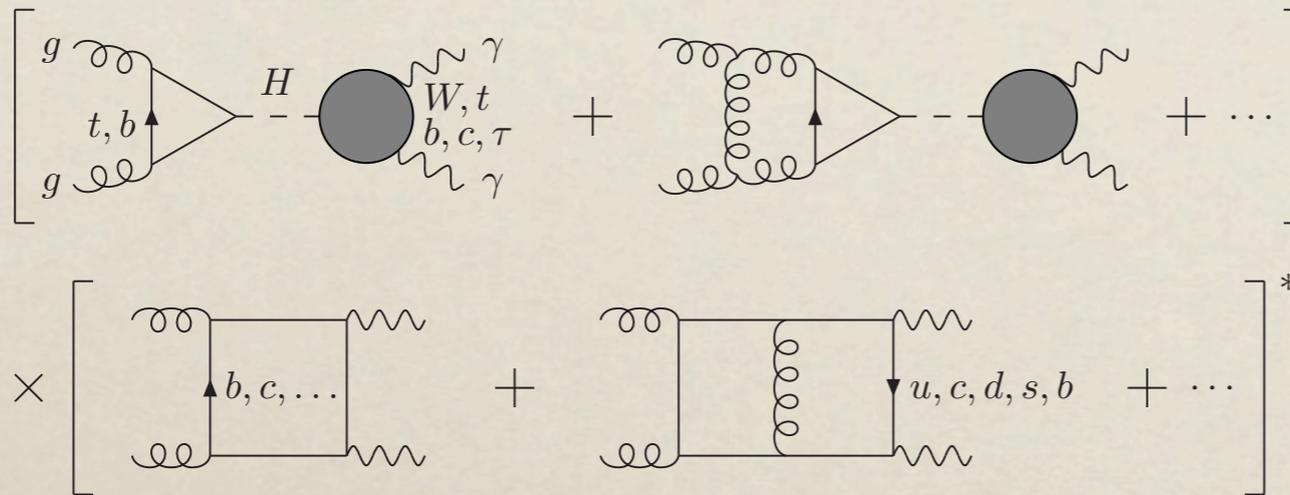
$$\begin{aligned} \mathcal{A}_{gg \rightarrow H} &\propto c_g \\ \mathcal{A}_{\gamma\gamma \rightarrow H} &\propto c_\gamma \end{aligned}$$

- *Higgs signal appears as resonance in diphoton invariant mass  $M_{\gamma\gamma}$  spectrum*
- *Finite detector resolution make direct measurement on Higgs width impossible*
- *The only observable: signal strength in narrow width approximation*

$$S \sim |\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H}|^2 \quad \sigma^{\text{sig}} = \int dM_{\gamma\gamma} \frac{S}{(M_{\gamma\gamma}^2 - m_H^2)^2 + m_H^2 \Gamma_H^2} \sim \frac{c_g^2 c_\gamma^2}{\Gamma_H} \rightarrow \text{Always appears as a combo!}$$

- *In SM, all Higgs properties dictated by  $m_H$ , how well can we test them at LHC?*
- *Need to decouple width from couplings*

# Interference



L.Dixon, M.Siu, hep-ph/0302233

- *Need to examine the width dependence of the interference*
- *The interference contribution*

$$-2m_H \Gamma_H \frac{\text{Im}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H} \mathcal{A}_{\text{cont}}^*)}{(M_{\gamma\gamma}^2 - m_H^2)^2 + m_H^2 \Gamma_H^2} - 2(M_{\gamma\gamma}^2 - m_H^2) \frac{\text{Re}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H} \mathcal{A}_{\text{cont}}^*)}{(M_{\gamma\gamma}^2 - m_H^2)^2 + m_H^2 \Gamma_H^2}$$

- *Integrated contribution of the interference term: suppressed by small Higgs width in size comparing to the pure signal*

$$\sigma^{\text{int}} = \int dM_{\gamma\gamma} \frac{(M_{\gamma\gamma}^2 - m_H^2)R + m_H \Gamma_H I}{(M_{\gamma\gamma}^2 - m_H^2)^2 + m_H^2 \Gamma_H^2} \sim c_g c_\gamma$$

$R \sim \text{Re}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H} \mathcal{A}_{\text{cont}}^*)$   
 $I \sim \text{Im}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H} \mathcal{A}_{\text{cont}}^*)$

# Interference

- *Interference has two pieces*

$$R \sim \text{Re}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H} \mathcal{A}_{\text{cont}}^*)$$
$$I \sim \text{Im}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H} \mathcal{A}_{\text{cont}}^*)$$

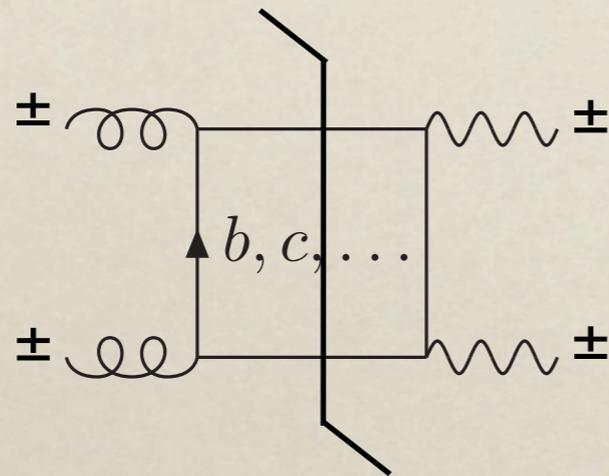
$$\sigma^{int} = \int dM_{\gamma\gamma} \frac{(M_{\gamma\gamma}^2 - m_H^2)R + m_H \Gamma_H I}{(M_{\gamma\gamma}^2 - m_H^2)^2 + m_H^2 \Gamma_H^2} \sim c_g c_\gamma$$

D.Dicus, S.Willenbrock, Phys.Rev.D37,1801

- *Real part of Breit-Wigner: asymmetric around Higgs peak, negligible contribution to integrated cross section given that R doesn't vary too quickly*
- *Imaginary part of Breit-Wigner: constructive or destructive contribution depending on the relative phase between signal and background*

# Imaginary part of Interference

$$\mathcal{A}^{\text{tree}}(g^\pm g^\pm \rightarrow q\bar{q}) = \mathcal{A}^{\text{tree}}(q\bar{q} \rightarrow \gamma^\pm \gamma^\pm) = 0 \text{ for } m_q = 0$$



$$I \sim \text{Im}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H} \mathcal{A}_{\text{cont}}^*)$$

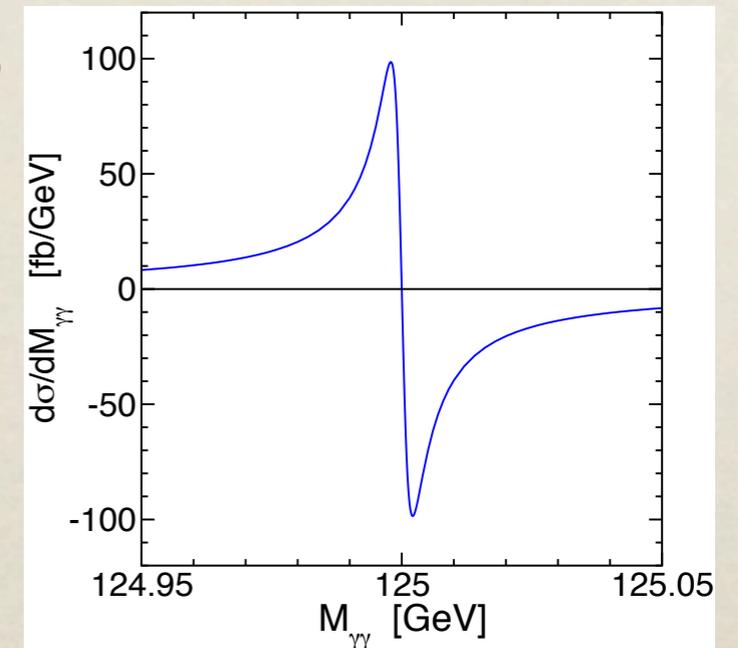
- *The full  $gg \rightarrow H \rightarrow \gamma\gamma$  signal amplitude is mainly real due to the dominant contribution from heavy top and W loops; contribution from light quark loops is suppressed by Yukawa couplings*
- *Need imaginary part from SM background for the relative phase*
- *SM continuum contribution starts at 1-loop*
  - *vanishing imaginary part in massless quark limit at LO*
- *Major imaginary part of SM background starts at 2-loop, leading to 1-2% destructive interference*
- *Too small an effect to see ...*

*Theoretical uncertainty on signal ~15%*

# LO Mass Shift

*Interference only (LO)*

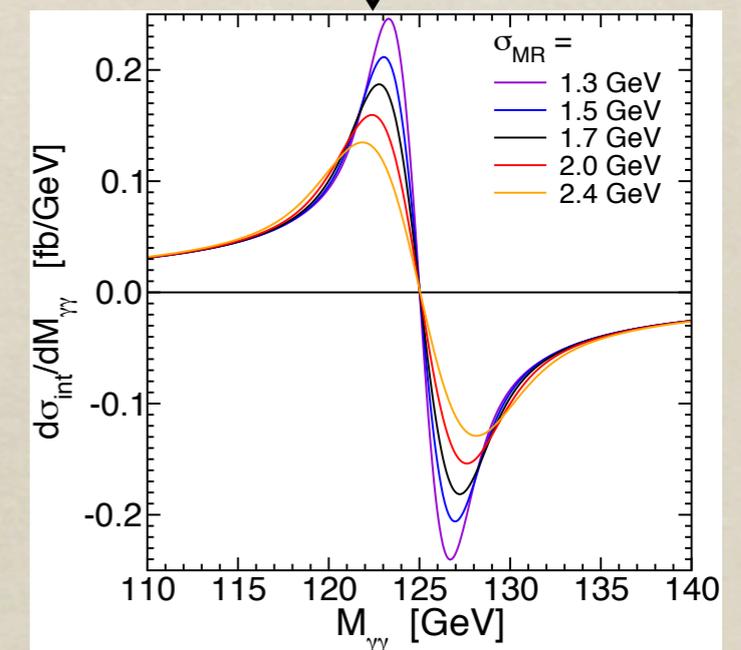
- *Real-part interference*
  - *non-vanishing at 1-loop with massless quarks*
  - *odd around Higgs mass  $\Rightarrow$  Higgs mass peak shift*
  - *generically, asymmetric shape peaks/dips at  $m_H \pm \Gamma_H/2 \Rightarrow$  mass shift  $\sim \Gamma_H$*



S.Martin, hep-ph/1208.1533

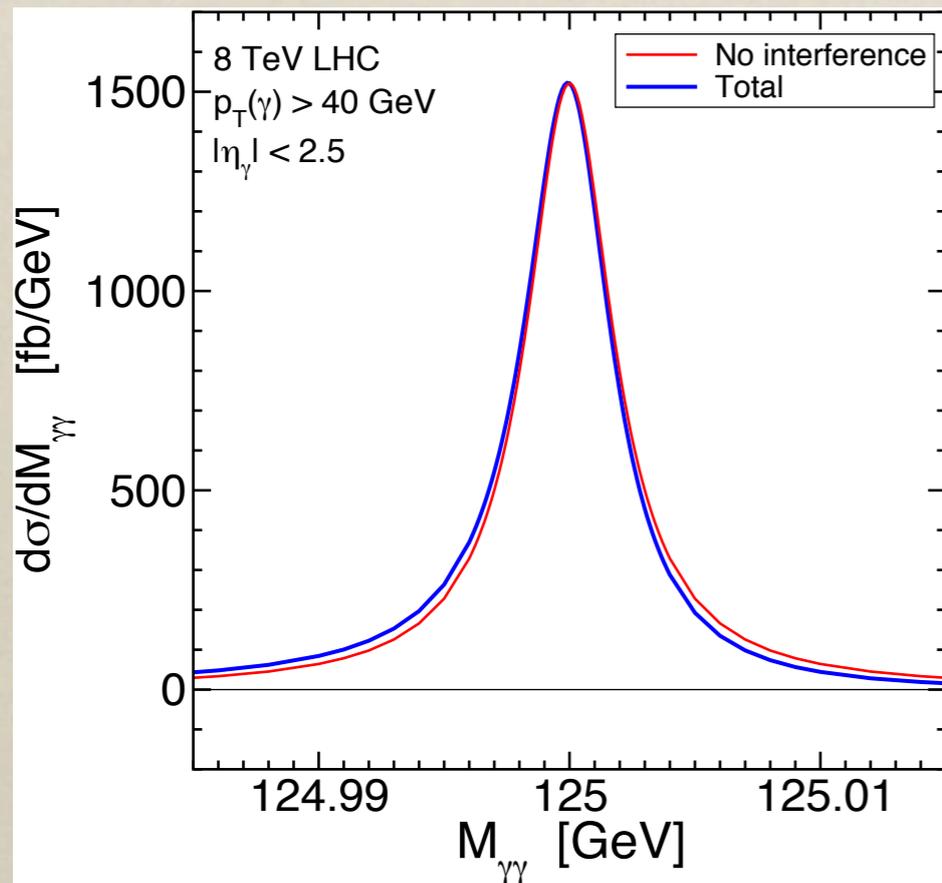
- *Different story when including effect of finite detector resolution*

- *considerable contribution from Breit-Wigner tails*
- *potentially visible shift of Higgs mass peak  $\sim 100$  MeV*

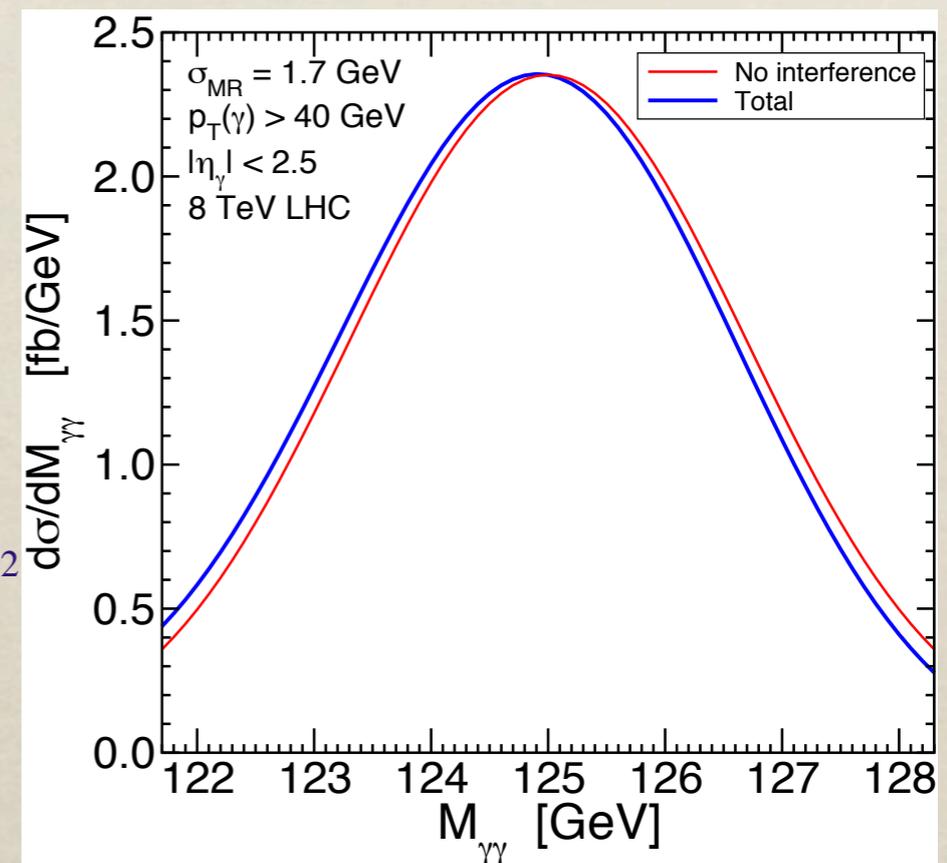


# LO Mass Shift

*illustration of how interference changes the diphoton invariant mass spectrum*



→  
S.Martin, hep-ph/1303.3342

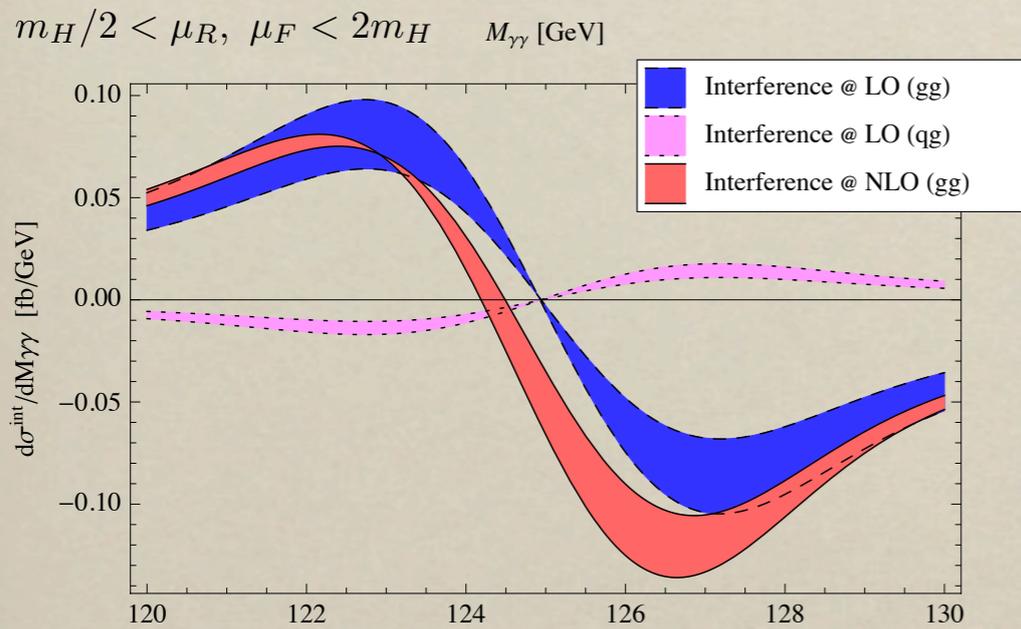
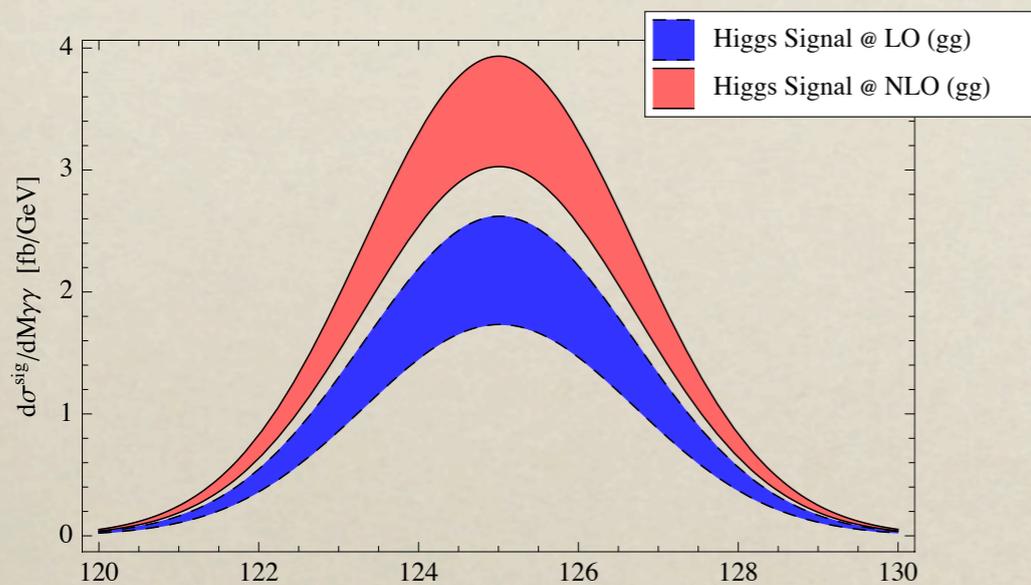


*diphoton spectrum in ideal detector*

*spectrum with detector mass resolution of 1.7 GeV*

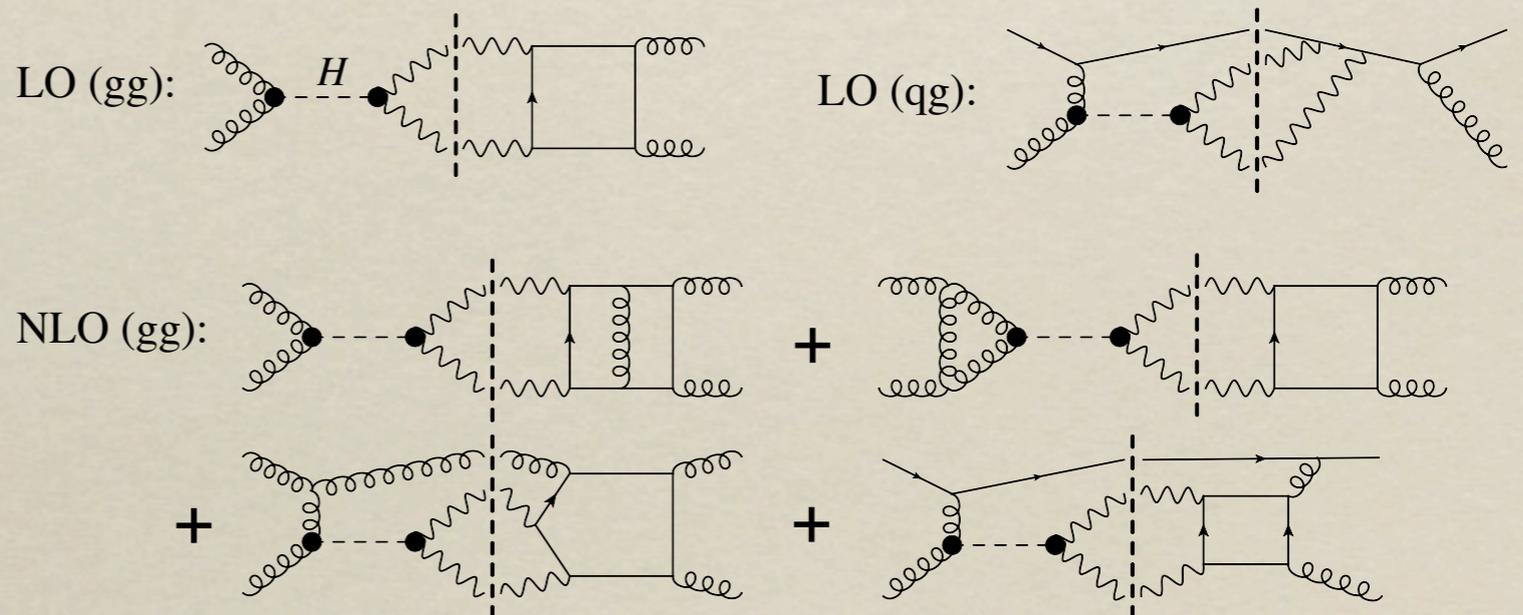
# NLO QCD Correction

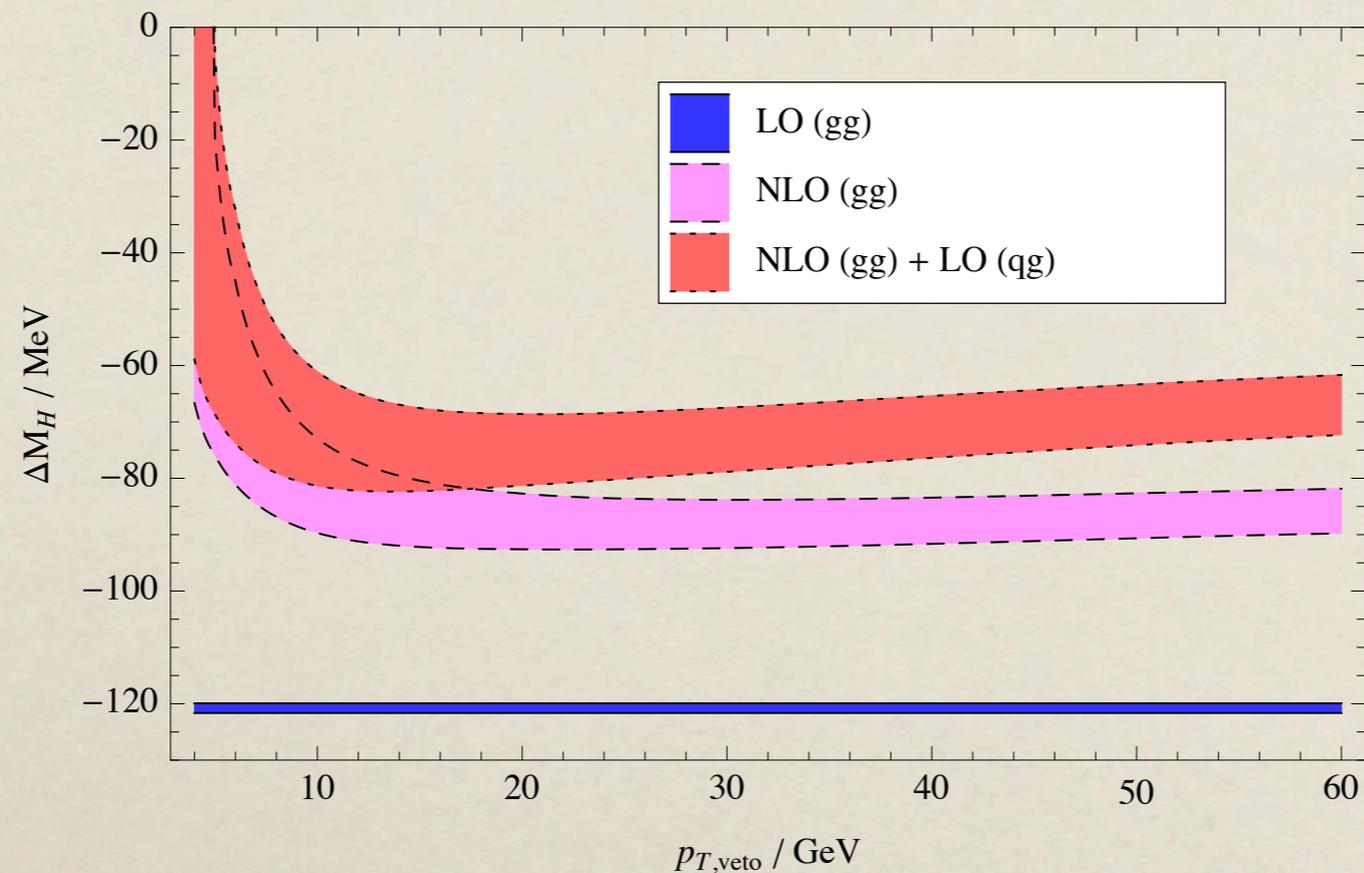
LHC @ 8 TeV  $\sigma_{MR} = 1.7 \text{ GeV}$



$p_{T,\gamma}^{\text{hard/soft}} > 40/30 \text{ GeV}, |\eta_\gamma| < 2.5$   
 Isolation:  $\Delta R_{\gamma j} < 0.4, p_{T,j} > 3 \text{ GeV}$   
 Veto jet :  $p_{T,j} > 20 \text{ GeV}, \eta_j < 3$

- Known large  $K$  factor of Higgs production and SM background in QCD at NLO
  - more uncertainty when  $p_T$  veto is involved
- Complicated  $K$  factor dependence on  $M_{\gamma\gamma}$  spectrum for interference due to interplay between the two parts
  - imaginary part interference starts at 2-loop and is small
  - real part interference receives a relative constant  $K$  factor ( $\sim 2$  for inclusive case) between that of pure signal ( $\sim 2.5$ ) and background ( $\sim 1.5$ )





- *smaller  $K$  factor compared to signal  $\Rightarrow$  reduced mass shift*
- *with radiation, the extra contribution from the interference with tree level diagram in quark gluon channel,  $LO(qg)$ , partly cancels with interference of gluon gluon channel,  $(N)LO(gg)$   $\Rightarrow$  further reduces mass shift*
- *mostly insensitive to  $p_T$  veto choice because of large contribution from virtual correction*

# Bounding Higgs Width

- Mass shift sensitive to Higgs width due to modified couplings

- must **keep constant signal yields** to be consistent with current experimental observation

$$c_{g\gamma} = c_g c_\gamma$$

$$\frac{c_{g\gamma}^2 S}{m_H \Gamma_H} + c_{g\gamma} I = \left( \frac{S}{m_H \Gamma_H^{SM}} + I \right) \mu_{\gamma\gamma}$$

ratio of experimental signal strength to SM prediction

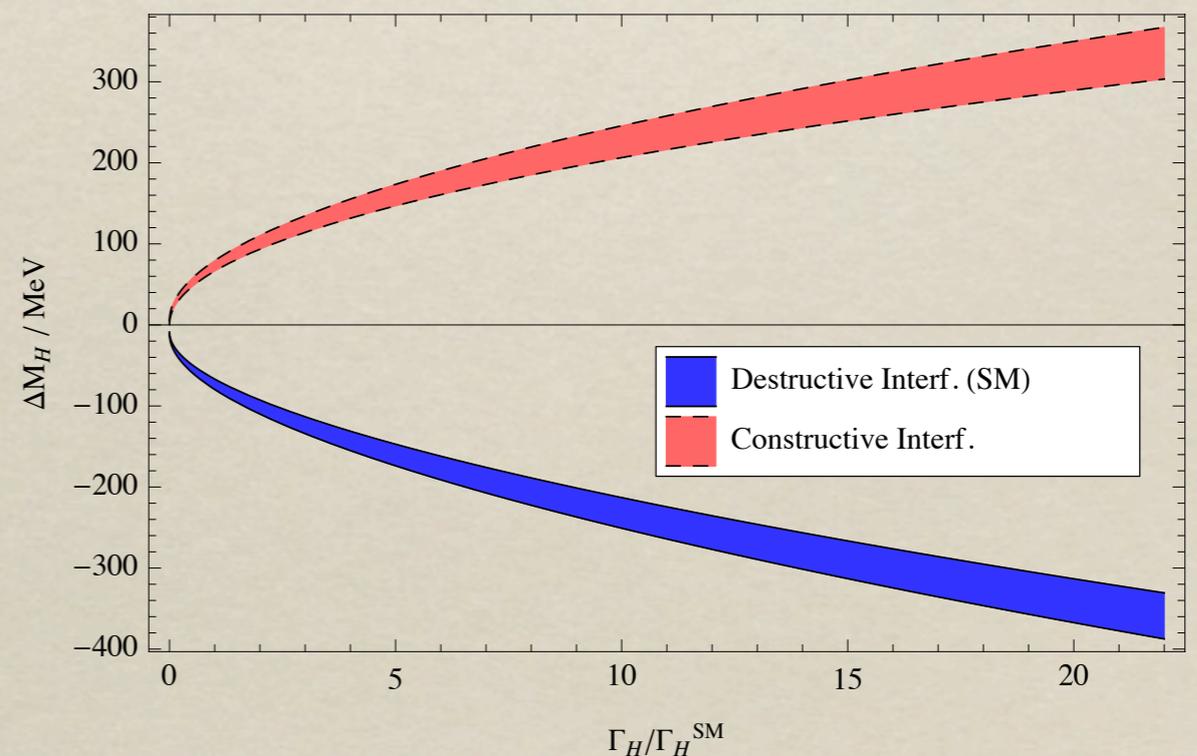
- simple solution if vanishing destructive (constructive) interference

$$|\Delta m_H| \sim |c_{g\gamma}| = \sqrt{\Gamma_H / \Gamma_H^{SM}}$$

for  $\mu_{\gamma\gamma} = 1$

- In case NP flips the sign of Higgs amplitude  $\Rightarrow$  Constructive Interference

- Complement to ILC in constraining Higgs width!



# Probing Mass Shift

- Need a reference channel to measure the shift:

N.Kauer, G.Passarino, hep-ph/1206.4803

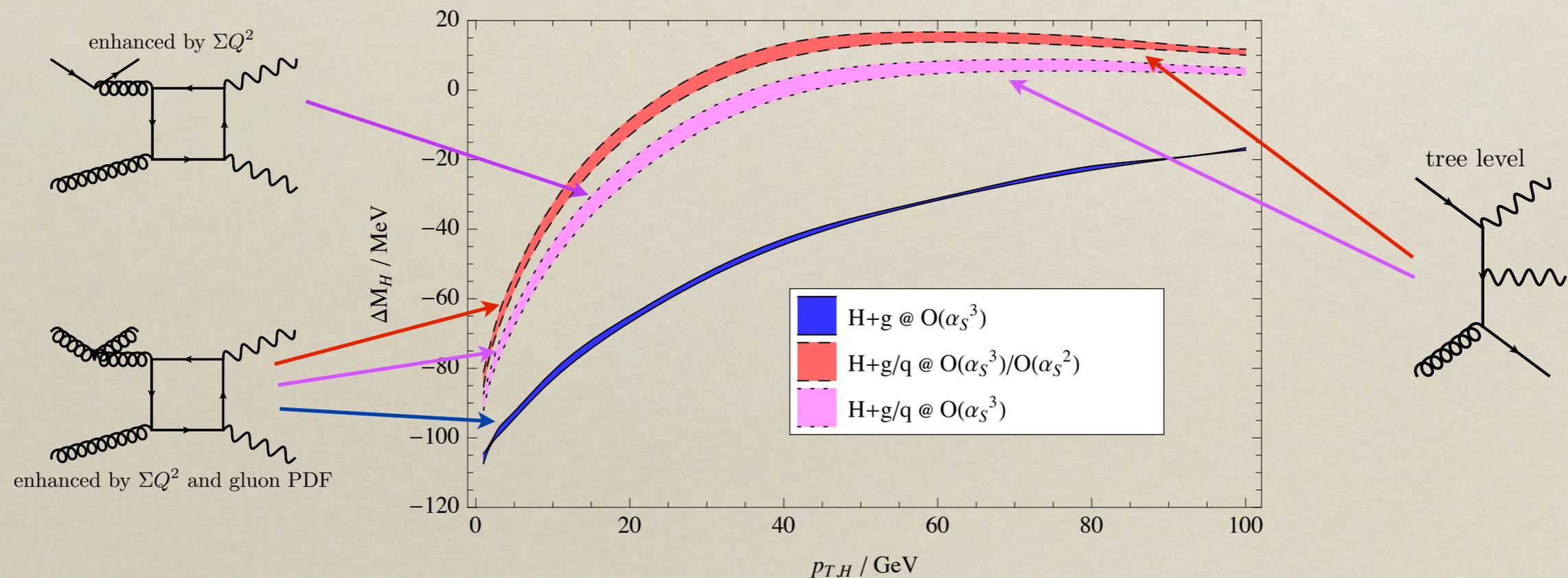
- $ZZ^*$  channel where interference near Higgs resonance is negligible
  - Possible large systematic errors as current ATLAS and CMS results incompatible

$$m_H^{\gamma\gamma} - m_H^{ZZ} = +2.3_{-0.7}^{+0.6} \pm 0.6 \text{ GeV (ATLAS)}$$

$$= -0.4 \pm 0.7 \pm 0.6 \text{ GeV (CMS),}$$

S.Martin, hep-ph/1303.3342

- Cancellation between  $qg$  and  $gg$  channels results in **strong dependence on Higgs  $p_T$**   $\Rightarrow$  virtually no mass shift on high  $p_T$  events



# Constraining the Width

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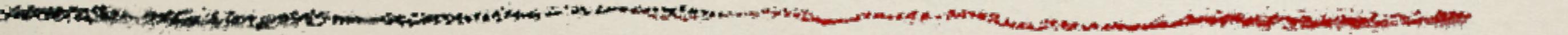
- *Potentially able to measure mass shift using two Higgs  $p_T$  bins*
  - *Better choice because experimental systematic uncertainty may cancel to some extent; still limited by statistics at present*
  - *At high luminosity LHC with  $3 \text{ ab}^{-1}$  data, statistical error on mass shift should drop to below 50 MeV; while the extrapolation of systematic error is somewhat uncertain but should result in a total error of 100 MeV or less, corresponding to a bound of Higgs width of around 15 times that of SM value (4 MeV) at 95% C.L.*

# Conclusion

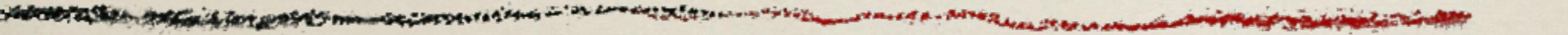
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- *Part of Higgs signal and background interference proportional to real part of BW propagator yields potentially observable mass shift with finite detector resolution*
- *The mass shift survives at NLO in QCD, allowing possibility to study the interference experimentally, and decouple the Higgs width and coupling measurements*
- *Increasing Higgs width leads to considerably larger mass shift which can be used to bound the width*
- *Strong dependence of mass shift on finite Higgs  $p_T$  provides way of probing it without reference to  $ZZ^*$  decay channel*

Thank you !



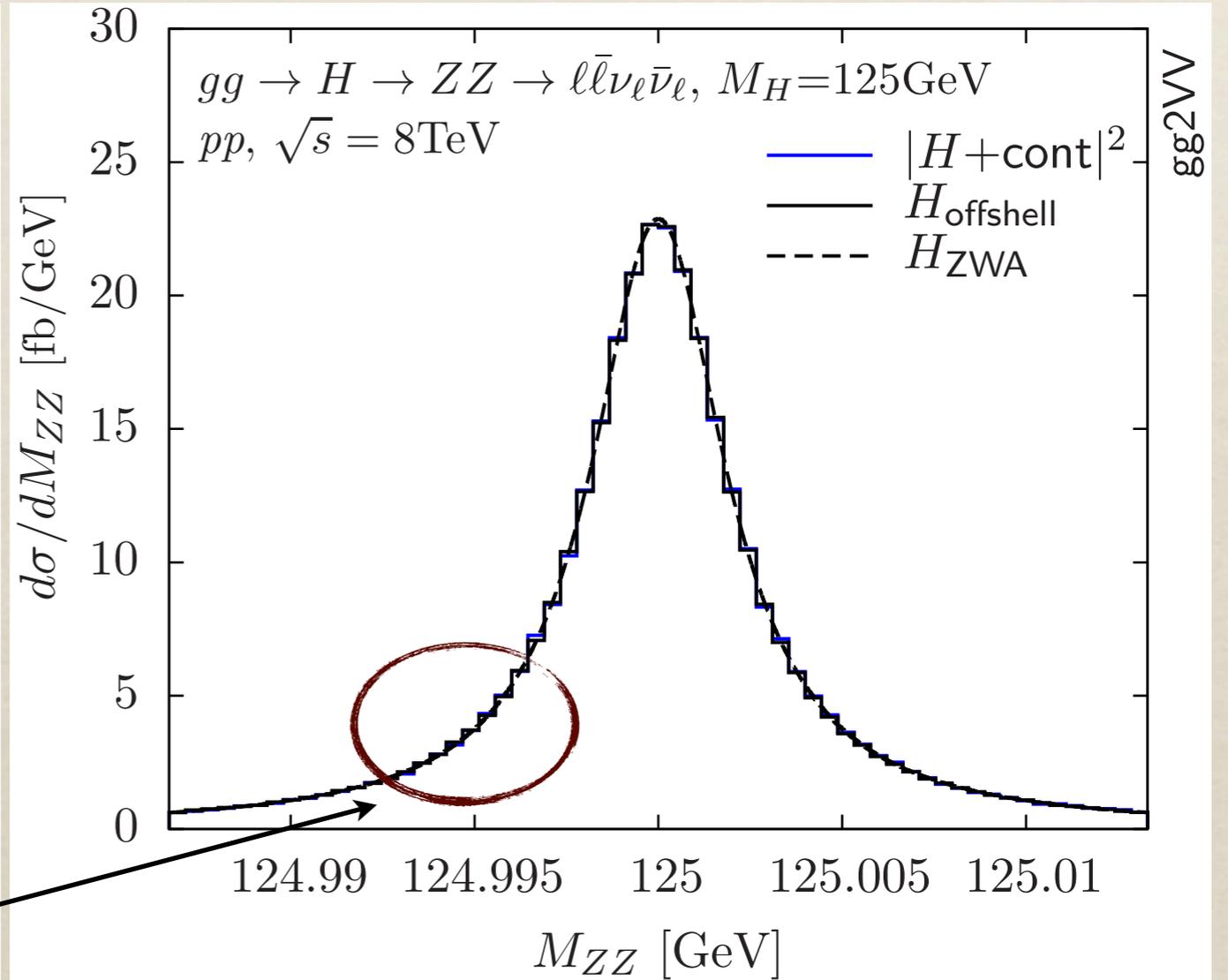
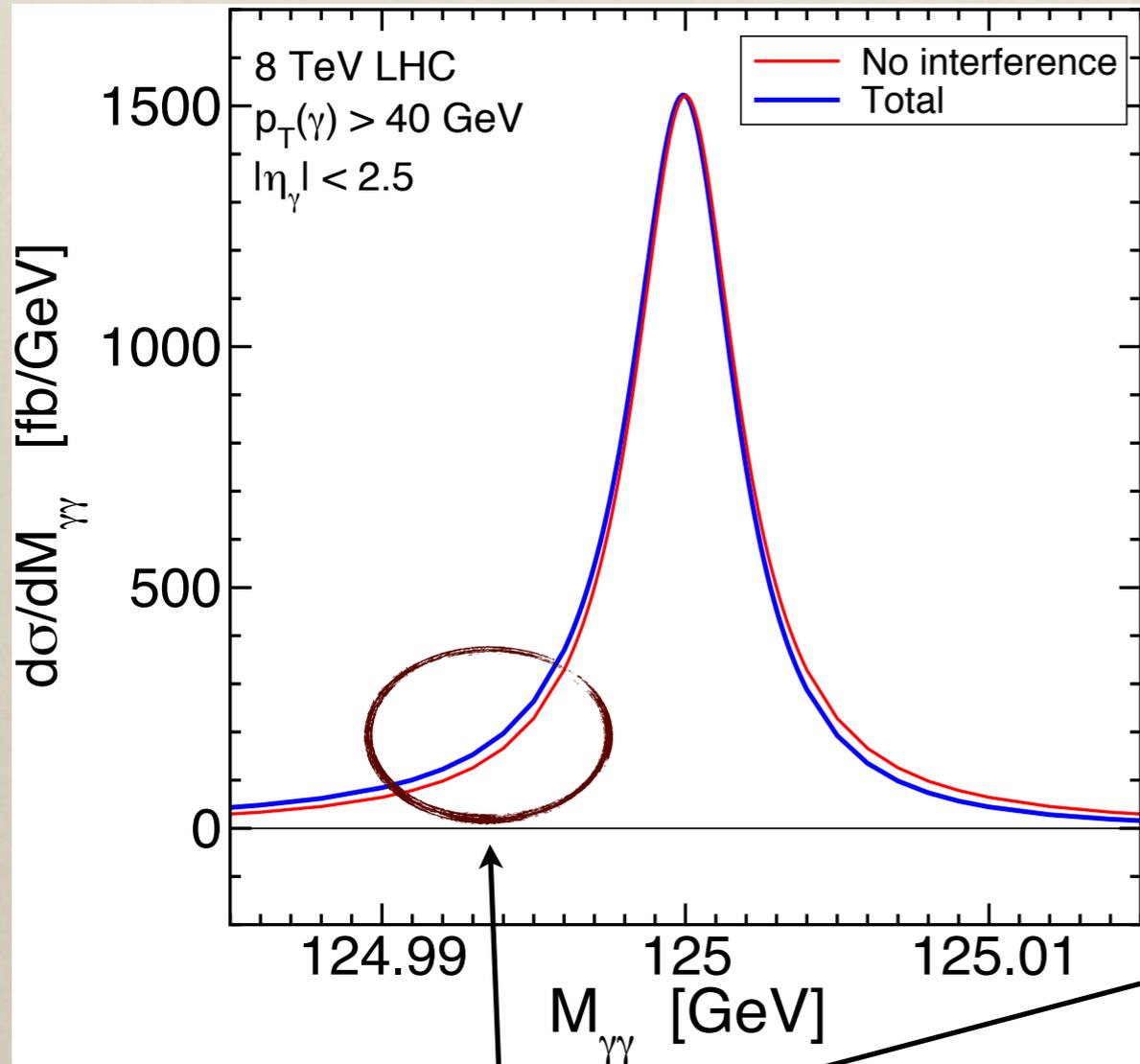
Backup slides



# Interference in ZZ and $\gamma\gamma$

S.Martin, hep-ph/1303.3342

N.Kauer, G.Passarino, hep-ph/1206.4803



*interference  
 in ZZ is very  
 small*

*The mass measurement can be approximated by a least square fit of the mass peak, which can be shown via likelihood analysis by assuming a relatively constant and well-modeled background in the mass range of consideration*

# Higgs in Mixed CP State

- *New CP-odd couplings in the effective Lagrangian*

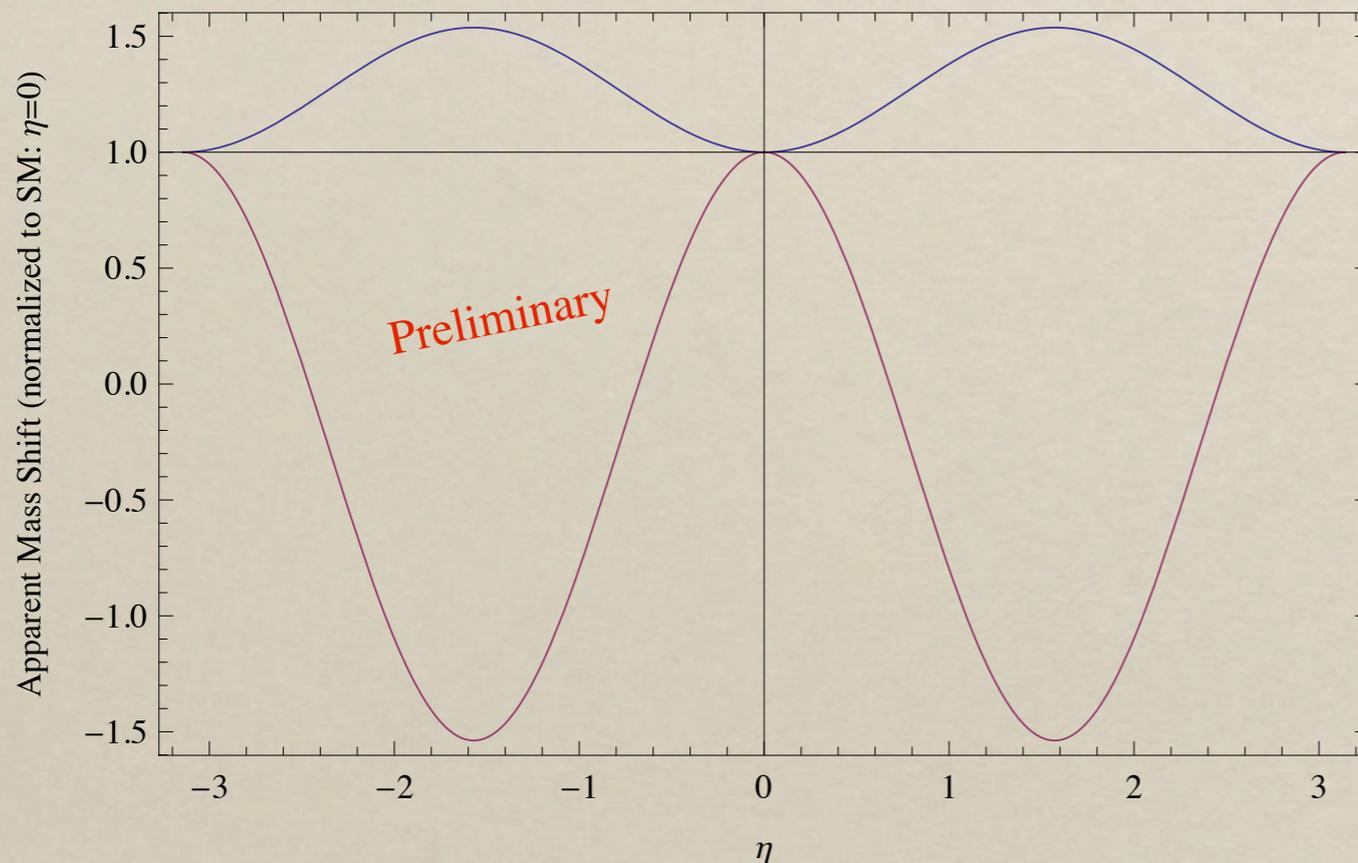
$$\mathcal{L} = - \left[ \frac{\alpha_s}{8\pi} (c_g b_g G_{a,\mu\nu} G_a^{\mu\nu} + s_g d_g G_{a,\mu\nu} \tilde{G}_a^{\mu\nu}) + \frac{\alpha}{8\pi} (c_\gamma b_\gamma F_{\mu\nu} F^{\mu\nu} + s_\gamma d_\gamma F_{\mu\nu} \tilde{F}^{\mu\nu}) \right] \frac{h}{v}$$

- *In SM,  $c_{g/\gamma}=1$  is reserved for adjusting couplings for Higgs in mixed CP state;  $b_{g/\gamma}$  is given via matching from full theory;  $s_{g/\gamma}d_{g/\gamma}=0$  when Higgs is a CP-even scalar*
- *$s_{g/\gamma}$  is reserved for the same purpose as  $c_{g/\gamma}$*
- *Define  $d_{g/\gamma}$  so that when we turn off original CP-even coupling ( $c_{g/\gamma}b_{g/\gamma}=0$ ) and set  $s_{g/\gamma}=1$ , the total cross section of SM Higgs signal is reproduced  $\Rightarrow d_{g/\gamma} = b_{g/\gamma}$  at LO*

# Higgs in CP Mixed State

- To keep constant signal yield, it's not hard to find the solution:  $c_{g/\gamma}^2 + s_{g/\gamma}^2 = 1$ , naturally parametrized as  $c_{g/\gamma}, s_{g/\gamma} = \cos(\eta_{g/\gamma}), \sin(\eta_{g/\gamma})$ 
  - If we treat the two CP phases ( $\eta_g, \eta_\gamma$ ) independently, the interference could change signs, resulting in positive mass shift
  - The mass shift is roughly 1.5 times stronger in pure CP-odd case compared to CP-even case at LO, though CP-odd case strongly disfavored experimentally

pure CP-odd:  $\eta_{g,\gamma} = \pm \frac{\pi}{2}$



- NLO effect is hard to tell (depending on the full theory giving rise to the CP-odd couplings) but is expected to increase signal and interference both as in the SM case

—  $\eta = \eta_g = \eta_\gamma$

—  $\eta = \eta_g = -\eta_\gamma$

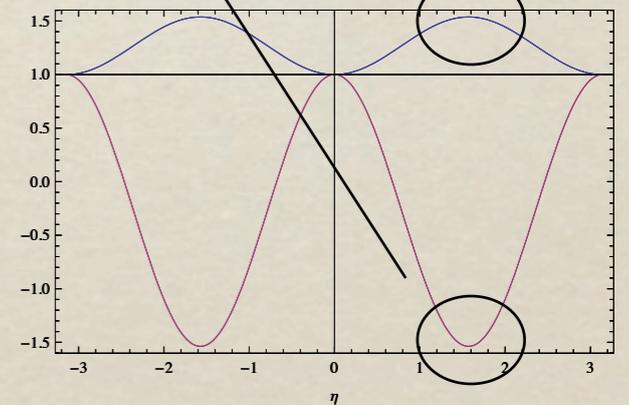
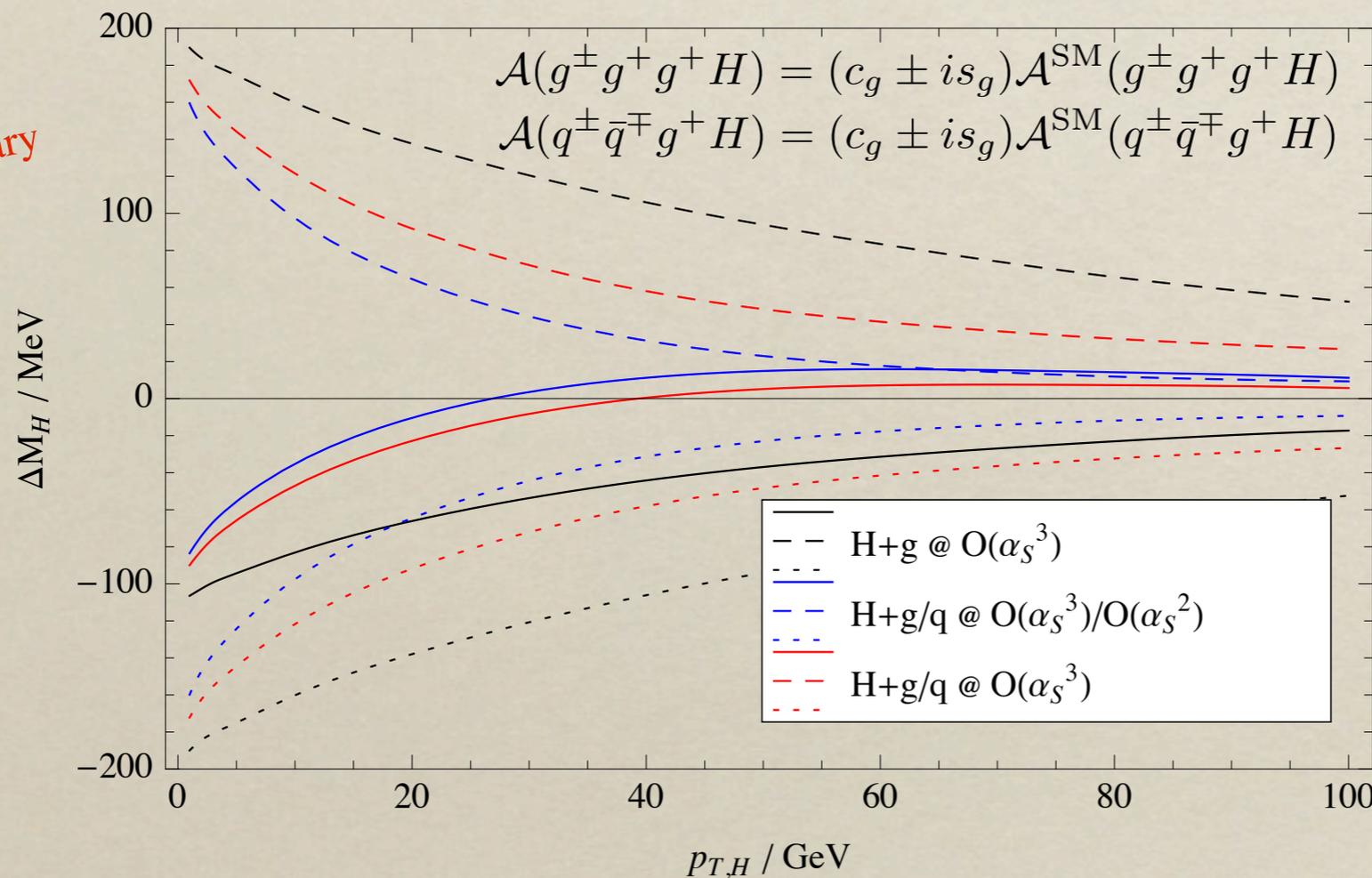
$$\mathcal{A}(g^\pm g^\pm H) = (c_g \pm i s_g) \mathcal{A}^{\text{SM}}(g^\pm g^\pm H)$$

$$\mathcal{A}(\gamma^\pm \gamma^\pm H) = (c_\gamma \pm i s_\gamma) \mathcal{A}^{\text{SM}}(\gamma^\pm \gamma^\pm H)$$

# Higgs with Finite pT

- *The mass shift dependence of finite pT as CP phases vary has similar behavior to the zero pT case*
  - *solid line is for SM; dotted line is for  $c_{g/\gamma}=0, s_g=s_\gamma=1$ ; dashed line is for  $c_{g/\gamma}=0, s_g=-s_\gamma=1$*
  - *mass shift no longer crosses 0 in pure CP-odd case*

Preliminary



*tree level  
analysis  
only*

# Higgs with Spin-2

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- *The interference btw signal and background occurs with different helicity configurations (compared to spin-0 case)*
  - *Gluon and photon pairs have opposite helicity due to spin conservation*
  - *Thus non-vanishing imaginary part of SM background amplitude in massless quark limit at LO*
- *Graviton-like: photon and gluon couples to spin-2 particle via stress energy tensor*
  - *Dictates couplings to photon and gluon with the same sign*
  - *Also discuss couplings with different signs here for completeness*
  - *Direct coupling of H to quarks not included as it's small for graviton-like case*

# Signal vs. Interference

$$|\overline{\mathcal{A}}|^2 = \left[ \frac{G_{g\gamma}^2}{256} f_0(c) + \pi \xi M \Gamma f_i(c) \right] \frac{1}{(\hat{s} - M^2)^2 + M^2 \Gamma^2} + \frac{\xi f_r(c)}{(\hat{s} - M^2)^2 + M^2 \Gamma^2} \frac{\hat{s} - M^2}{1}$$

$c = \cos \theta$   
 $\xi = \frac{11}{72} G_{g\gamma} \alpha \alpha_s$

Interference - real part

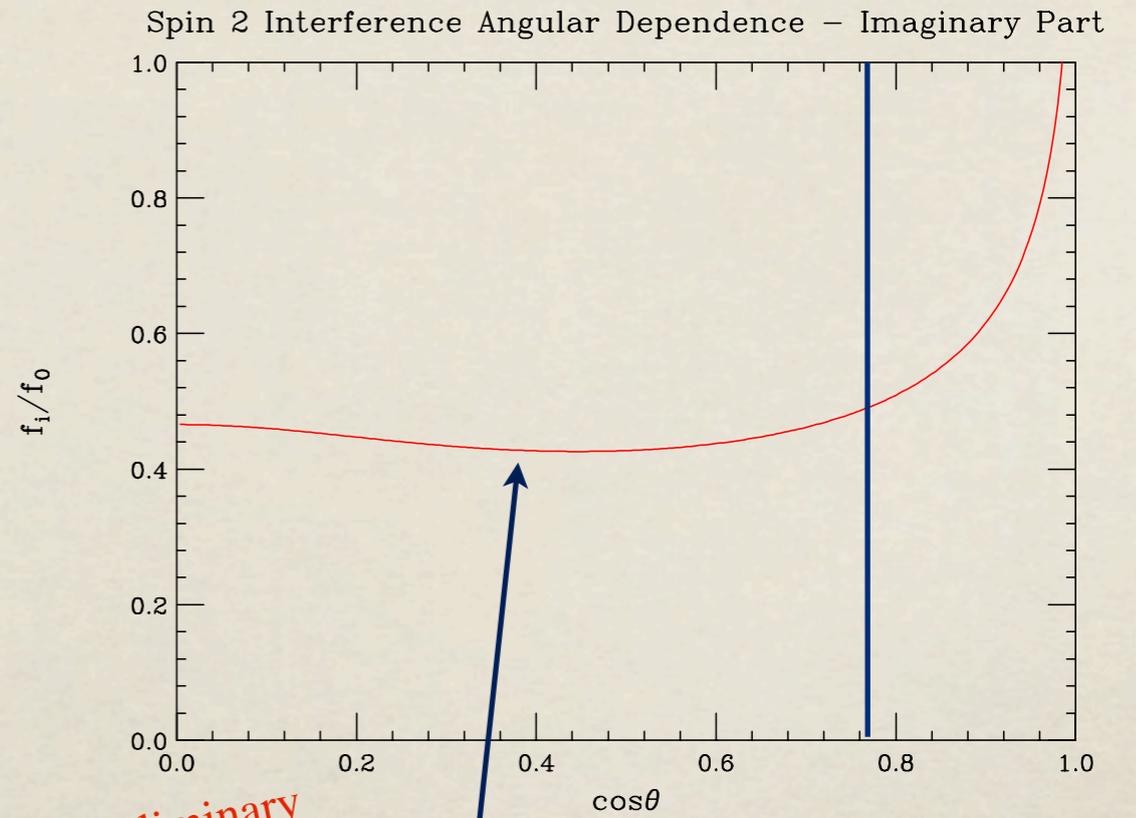
Signal      Interference - imaginary part

- Normalize the spin-2 coupling so that signal yield is the same as the SM Higgs
- Need non-zero photon  $p_T$  cut for finite interference contribution in spin-2 case
- Choose  $p_{T\text{cut}} = 40 \text{ GeV}$  to solve for  $G_{g\gamma}$  by equating the yields for spin-0 and spin-2
- Moderate  $p_T$  cut (40 GeV) limits photon to central region where interference and signal has relatively similar angular dependence

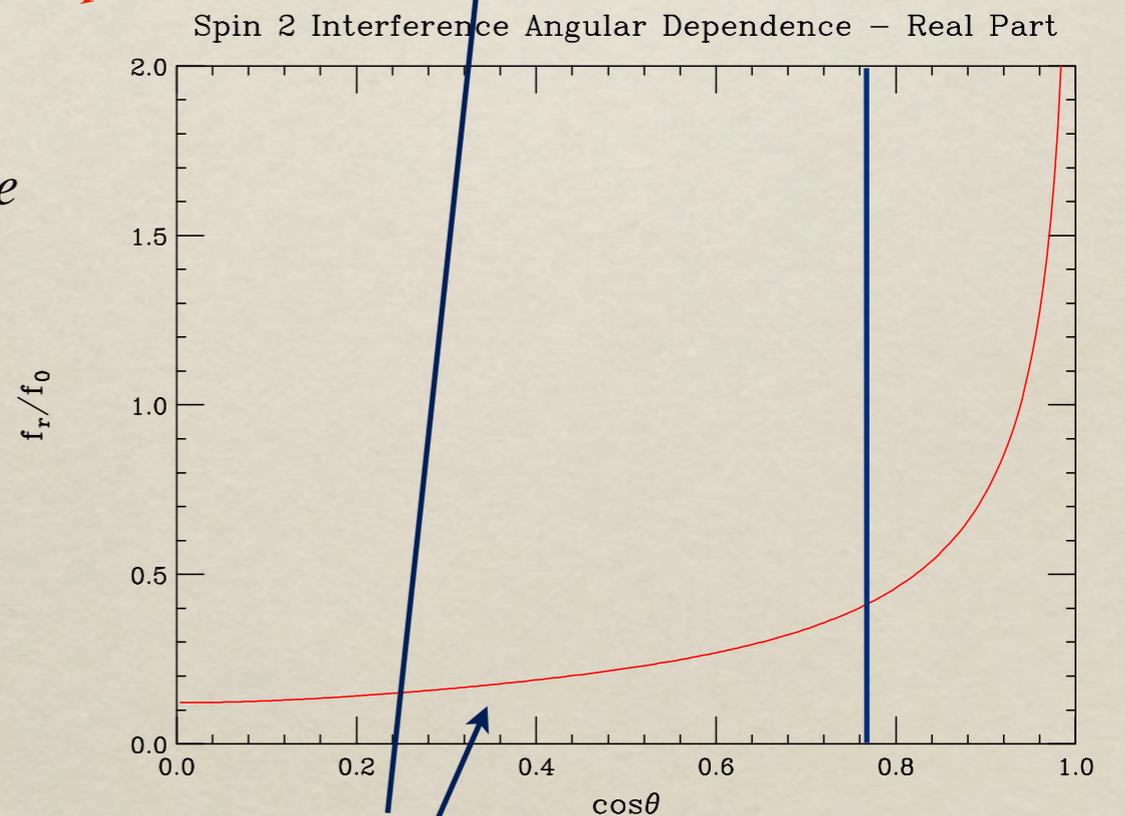
$$\cos \theta_{max} = \sqrt{1 - 2(p_T^{cut}/M_{\gamma\gamma})^2} \xrightarrow{p_T^{cut}=40\text{GeV}} 0.77$$

- signal-only angular distribution analysis largely unaffected by interference contribution

$G_{g\gamma} > 0$  for heavy graviton



Preliminary

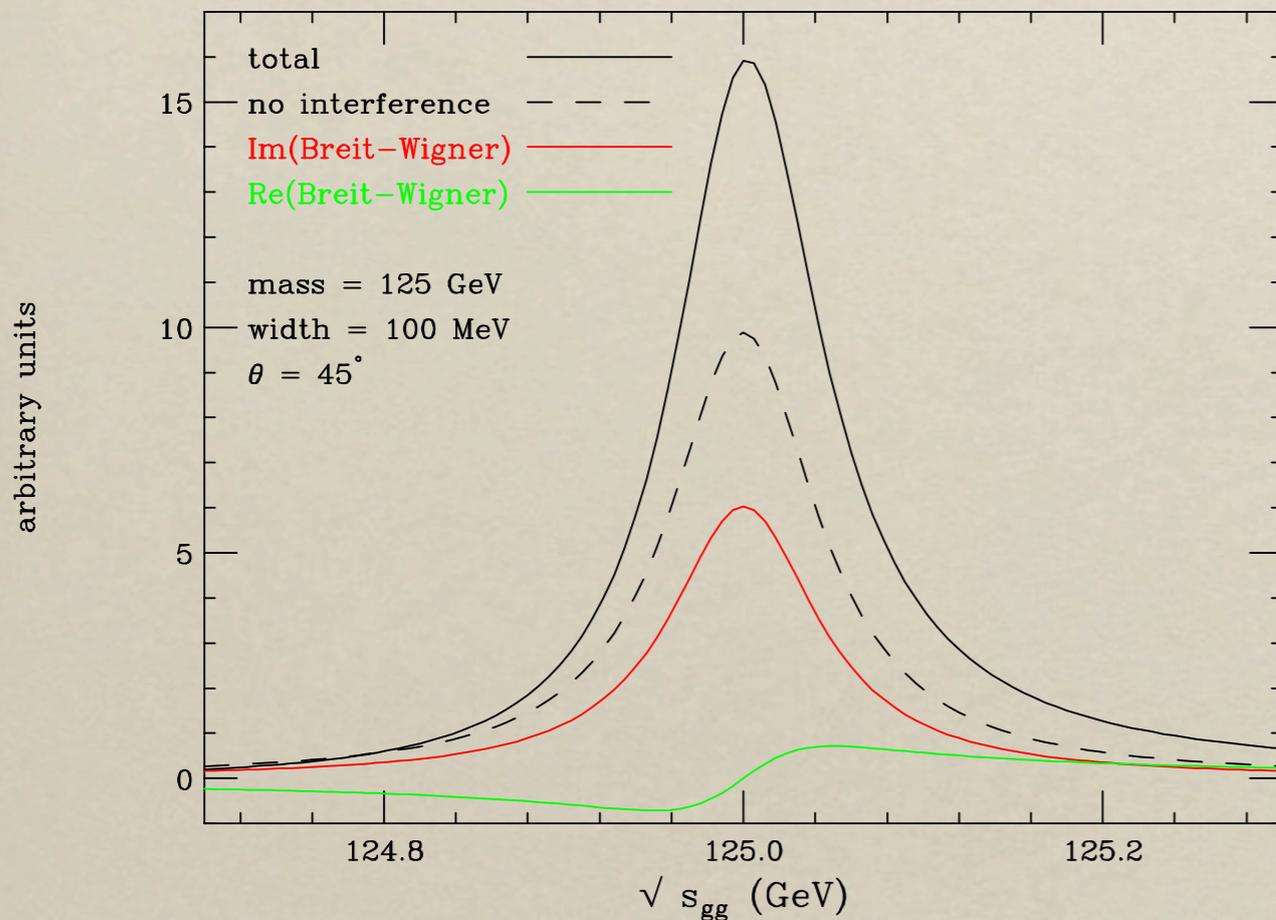


almost flat profile for small scattering angle

# Interference on Signal Yields (Spin-2)

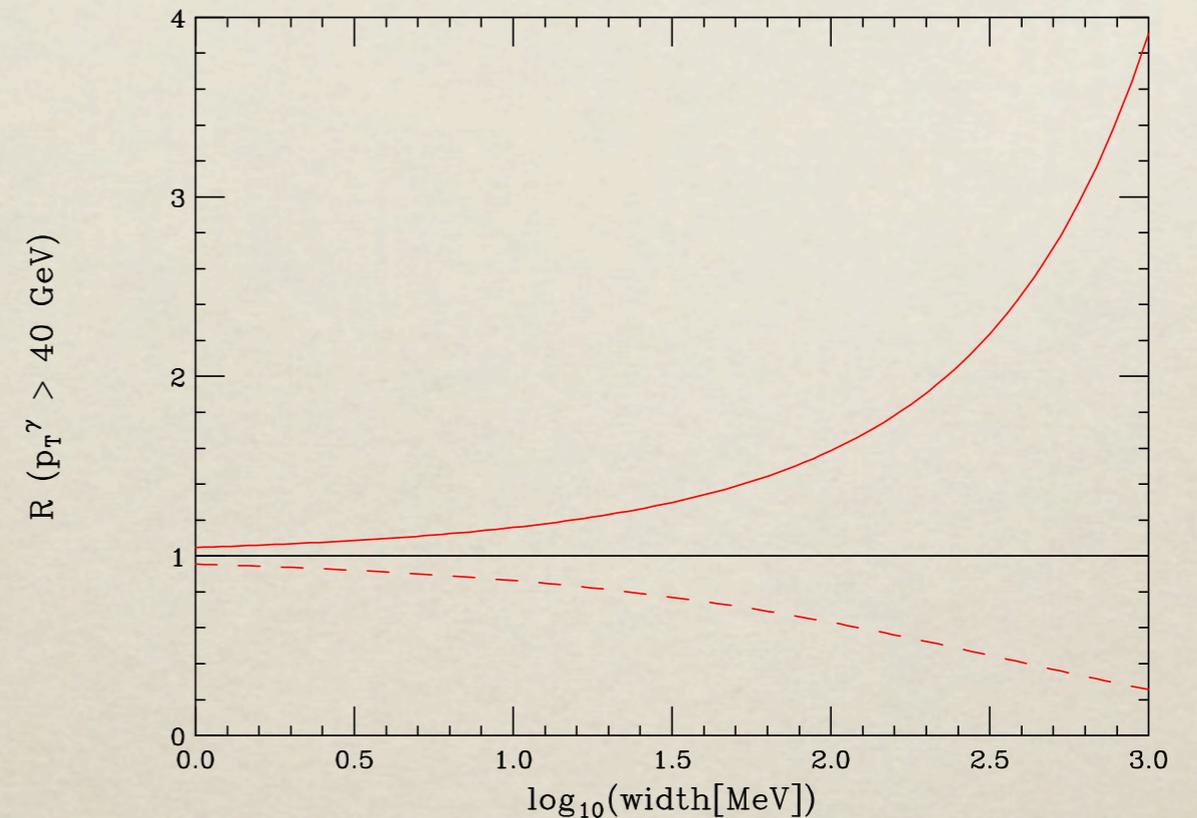
- *Strong constructive/ destructive interference at large width because imaginary part interference starts at LO*

$gg \rightarrow G \rightarrow \gamma\gamma$  Lineshape



Preliminary

Interference Correction to Event Rate



- *for  $\Gamma = 100 \text{ MeV}$  :  $O(1)$  correction to signal yields ( $\sim 50\%$ )*
- *Affect the coupling measurement in spin-2 interpretation*